1)[5pts] Find all solutions to the differential equation y'' - 4y' + 7y = 0.

The characteristic equation is $r^2 - 4r + 7 = 0$. The solutions to this are $r = \frac{1}{2}(4 \pm \sqrt{16 - 28}) = 2 \pm i\sqrt{3}$. Therefore, any solution to the differential equation is of the form $c_1e^{2t}\sin(t\sqrt{3}) + c_2e^{2t}\cos(t\sqrt{3})$.

2)[5pts] Find all solutions to y''' + 7y'' = 0, and find a particular solution such that y(0) = 0 and y'(0) = 1. (Hint: there are infinitely many to choose from, but I just want one)

The characteristic equation is $r^3 + 7r^2 = r^2(r+7) = 0$, so the general solution is of the form $c_1e^{-7t} + c_2e^{0t} + c_3te^{0t} = c_1e^{-7t} + c_2 + c_3t$. If we take $c_1 = c_2 = 0$ and $c_1 = 1$, we have y(t) = t, which satisfies y(0) = 0 and y'(0) = 1.