

EVANS 03

#9 let u and v be parametric curves
in \mathbb{R}^3 that satisfy

$$\begin{aligned} u' &= v - u & ' &= \frac{d}{dt} \\ v' &= v + u \end{aligned}$$

Show that $u \times v = \text{constant}$

$$\frac{d}{dt} u \times v = 0$$

$$u' \times v + u \times v' = 0$$

Cross product
identities

$$(v - u) \times v + u \times (v + u) = 0$$

$$\underbrace{v \times v}_0 - \underbrace{u \times v} + \underbrace{u \times v} + \underbrace{u \times u}_0 = 0$$

$$\boxed{0 = 0}$$